I PUC MID-TERM EXAMINATION, OCTOBER-2023 (SET-1)

Time : 3 Hrs. 15 Mins. **SUBJECT : BASIC MATHEMATICS (75)** **Max Marks : 80**

Instructions :
1) The question paper has 5 parts A, B, C, D and E. Answer all the parts.
2) Part-A carries 20 marks, Part-B carries 12 marks, Part-C carries 15 marks, Pard-D carries 25 marks and Part-E carries 8 marks.
3) Write the question number properly as indicated in the question paper in the margin.

PART - A

I **Choose the correct answer (Each question carries 1 mark) :** 5x1=5

1) The number of positive divisors of 60 are
   a) 21　　　　b) 12　　　　c) 6　　　　d) 16

2) $\left(x^{1/2} + y^{1/2}\right) \cdot \left(x^{1/2} - y^{1/2}\right) =$
   a) $x - y$　　　b) $x + y$　　　c) $\sqrt{x} - \sqrt{y}$　　　d) $\sqrt{x} + \sqrt{y}$

3) The value of cos A.cosec A is
   a) cos A　　　b) sin A　　　c) tan A　　　d) cot A

4) The value of tan 225° is
   a) -1　　　b) $\sqrt{3}$　　　c) 1　　　d) $\dfrac{1}{\sqrt{3}}$

5) The reflection of $(4, -8)$ with respect to y-axis is
   a) $(-4, 8)$　　　b) $(4, 8)$　　　c) $(-4, -8)$　　　d) $(4, -8)$

II **Match the following :** 5x1=5

6)
   i) $\left(\dfrac{5x^3}{y}\right)^2$ 　　　　　　　a) 96

   ii) $\log_2 \dfrac{1}{2} =$ 　　　　　　b) 0.08

   iii) 6th element of GP. 3, 6, 12, ... is 　　c) 157.5 $^\vee$
   iv) 8% in decimal form is 　　　　d) -1

   v) $\dfrac{7\pi}{8}$ in degrees is 　　　　e) $\dfrac{5x^6}{y^2}$

   　　　　　　　　　　　　　　f) 0.8

III **For the question numbers 7 to 11, choose the appropriate answer from the answer given in the bracket** 5x1=5

$$\left[-1, 5, \ 0.64, \ 64, \ 1 \ \dfrac{6}{10}\right]$$

7) The imaginary part of the complex number 3 + 5i is _____.
8) If $\log_{0.1} 10 = x$, then x is _____.

9) If $\dfrac{1}{3}$, x, $\dfrac{3}{2}$ are in HP, then x is _____.

10) If x% of 125 is $\dfrac{4}{5}$, then the value of x is ____.

11) The value of $(1 + \tan^2 A) \cdot \cos^2 A$ is ____.

(P.T.O.)

IV   Answer the following questions :   5x1=5

12) Express $2^5 = 32$ in the logarithmic form.

13) The first term of an AP is 3 and the common difference is -2. Find the 11th term.

14) Prove that $\sin A \cdot \sec A = \tan A$.

15) Find the value of $\sec \dfrac{7\pi}{3}$.

16) Find the equation of the locus of a point which moves such that the sum of its distance from co-ordinate axes is 5.

PART -B

V   Answer any SIX of the following questions :   6x2=12

17) Find the HCF of 55 and 210.

18) Simplify : $\dfrac{2^{7b-2a} \cdot 8^{2a-b}}{16^{a+b}}$.

19) Find the number of digits in the integral part of 3^{20}.

20) How many terms of the G.P. 1, 3, 9, ... will amount to 364 ?

21) When 40% of a number is added to 42, the result is the number itself. Find the number.

22) The S.P. of an article is ₹ 3680 and profit percent is 15%. Find the cost price.

23) Prove that $\tan^2 A + \sec^2 B = \sec^2 A + \tan^2 B$. https://www.karnatakaboard.com

24) Prove that $\left(\sin^2 \theta \cdot \cot^2 \theta\right) + \left(\cos^2 \theta \cdot \tan^2 \theta\right) = 1$.

25) If $A = 30°$. Verify that $\sin 2A = \dfrac{2 \tan A}{1 + \tan^2 A}$

26) Find the co-ordinates of the point P which divides the line joining the points $(-1, 2)$ and $(5, -7)$ in the ratio $3 : 4$ internally.

27) A point P moves such that $PA^2 = 3PB^2$. If $A = (5, 0)$ and $B = (-5, 0)$. Find the equation of the locus of P.

PART - C

VI   Answer any FIVE of the following questions :   5x3=15

28) Prove that $\sqrt{5}$ is an irrational number.

29) Simplify $\sqrt[bc]{\dfrac{x^b}{x^c}} \times \sqrt[ac]{\dfrac{x^c}{x^a}} \times \sqrt[ab]{\dfrac{x^a}{x^b}}$.

30) The sum of three numbers in AP is 15 and their product is 105. Find the numbers.

31) A sells a bicycle to B at a profit of 20% and B sells to C at a profit of 25%. If C pays ₹ 225 for the bicycle what did 'A' pay for it.

32) The difference of two angles is 45° and their sum is 90°. Find the angles in degrees and Radians.

33) Find the value of $3 \tan^2 30° + \dfrac{4}{3} \cos^2 30° - \dfrac{1}{2} \cot^2 45° - \dfrac{2}{3} \sin^2 60° + \dfrac{1}{8} \sec^4 60°$.

34) Find the equation of locus of a point such that the sum of its distance from $(0, 2)$ and $(0, -2)$ is 6.

PART - D

VII   Answer any FIVE of the following questions .   5x5=25

35) If $a^x = bc$, $b^y = ca$ and $c^z = ab$, show that $xyz = x + y + z + 2$.

36) Show that $\dfrac{y^{-1}}{x^{-1} + y^{-1}} + \dfrac{y^{-1}}{x^{-1} - y^{-1}} = \dfrac{2xy}{y^2 - x^2}$.

(P.T.O.)

37) If $m^2 + n^2 = 15mn$, show that $2 \log (m-n) = \log 13 + \log m + \log n$.

38) Using logarithmic tables find the value of $\dfrac{5.6348 \times 25.645}{12.72}$

39) A person buys a used car for ₹ 1,50,000 he pays ₹ 1,00,000 cash and agrees to pay the balance in annual installments of ₹ 5,000 plus 8% interest on the unpaid amount. How much will the Car cost for him ?

40) Venu gives 50% of his salary to his wife 40% of the remaining he spends on recreation 20% of the remaining he gives to his daughter as pocket money and still saves ₹ 12,000. What is Venu's income ? Also find the amount he gives his wife and daughter.

41) If $\tan A + \sin A = m$ and $\tan A - \sin A = n$ show that $(m^2 - n^2)^2 = 16mn$.

42) Simplify : $\dfrac{\sin 150° - 5\cos 300° + 7\tan 225°}{\tan 135° + 3\sin 210°}$

43) Show that the points $(-2, -1)$, $(1, 0)$, $(4, 3)$ and $(1, 2)$ are the vertices of a parallelogram

PART - E

VIII Answer any TWO of the following questions :   2x4=8

44) Find the sum of 'n' terms of the series 7 + 77 + 777 + ...

45) If $\tan A = -\dfrac{12}{5}$ and $270° < A < 360°$. Find the value of $\dfrac{3\sin A - 2\cos A}{9\cos A + 4\sin A}$.

46) For what value of 'a' the points $(1, 4)$, $(a, -2)$, $(-3, 16)$ are collinear.

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